

**NASA TECHNICAL
MEMORANDUM**

NASA TM X-64517

N 71-14636

NASA TMX 64517

**CRATER SIZE AND IMPACT FLASH PREDICTED FOR THE S-IV B
STAGE LUNAR IMPACT ON APOLLO 13 FLIGHT**

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December 10, 1970

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ACKNOWLEDGMENTS

The work performed by Charles MacKay, Billy Joe Taylor, and Byron R. Yance is greatly appreciated in accomplishing this study.

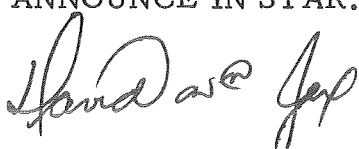
1. REPORT NO. TM X-64517		2. GOVERNMENT ACCESSION NO.		3. RECIPIENT'S CATALOG NO.	
4. TITLE AND SUBTITLE Crater Size and Impact Flash Predicted for the S-IVB Stage Lunar Impact on Apollo 13 Flight				5. REPORT DATE December 10, 1970	
				6. PERFORMING ORGANIZATION CODE	
7. AUTHOR (S) David W. Jex and Geoffrey Hintze				8. PERFORMING ORGANIZATION REPORT #	
9. PERFORMING ORGANIZATION NAME AND ADDRESS George C. Marshall Space Flight Center Marshall Space Flight Center, Alabama 35812				10. WORK UNIT NO.	
				11. CONTRACT OR GRANT NO.	
12. SPONSORING AGENCY NAME AND ADDRESS National Aeronautics and Space Administration Washington, D. C. 20546				13. TYPE OF REPORT & PERIOD COVERED Technical Memorandum	
				14. SPONSORING AGENCY CODE	
15. SUPPLEMENTARY NOTES Prepared by the Space Sciences Laboratory, Science and Engineering Directorate					
16. ABSTRACT <p>Marshall Space Flight Center has the responsibility to direct the impact of the S-IV B stage on the lunar surface during the Apollo 13 flight.</p> <p>The Space Sciences Laboratory conducted an investigation to determine the diameter of the crater expected and the intensity of the associated impact flash.</p> <p>Both theory and empirical relationships were used to obtain a meaningful conclusion.</p>					
17. KEY WORDS Lunar Impact Flash Crater Size S-IV B Stage Apollo 13 Flight			18. DISTRIBUTION STATEMENT ANNOUNCE IN STAR. 		
19. SECURITY CLASSIF. (of this report) Unclassified	20. SECURITY CLASSIF. (of this page) Unclassified	21. NO. OF PAGES 23	22. PRICE \$3.00		

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TECHNICAL MEMORANDUM X-64517

CRATER SIZE AND IMPACT FLASH PREDICTED FOR THE S-IV B STAGE LUNAR IMPACT ON APOLLO 13 FLIGHT

SUMMARY

An attempt was made to predict the crater size and impact flash created by the impact of the S-IV B stage of Apollo flight 13 on the lunar surface. Both theory and empirical relations were used to obtain a meaningful conclusion.

The crater diameter for the S-IV B stage impact was determined to be approximately 40 meters.

It was concluded that very small chances exist for observation of the impact flash from earth-based stations. The maximum flash expected would be on the order of a 16th magnitude star.

In the soil of two of the six laboratory impact craters glassy spheres were found similar to the spheres found in the Apollo 11 lunar soil sample.

INTRODUCTION

Marshall Space Flight Center has the responsibility to direct the impact of the S-IV B stage on the lunar surface during the Apollo 13 flight. The impact coordinates will be 3 degrees South, 30 degrees West, and impact time is predicted for 7:02 p.m. CST, on April 14, 1970.

Two questions connected with this impact arise: (1) What is the expected diameter of the crater that will be formed? and (2) Will the impact flash be observable from earth-based stations?

In order to answer these questions the Space Sciences Laboratory conducted the following investigations. To predict the diameter of the crater formed, an empirical explosive formula, missile impacts into different soils, and empirical tests in the light gas gun facility were employed. To determine if the flash generated by impact will be observable by earth-based stations, the impact of an aluminum projectile into a simulated lunar soil was monitored and analyzed.

CRATER SIZE

It has been observed that hypervelocity impact craters are similar to craters formed by explosives. An empirical expression [1] relating the size of the crater and energy is:

$$r^3 = k E \quad (1)$$

where r is the radius in feet, E is the energy of the explosive in pounds of TNT, and K is a constant which satisfies: $0.5 \leq k \leq 1.5$.

In the MKS system (International System of Units) r is the radius in meters, E is the energy in kilograms of TNT and k satisfies: $0.0312 \leq k \leq 0.0636$.

It has been found that one pound of TNT is equal to 1130 calories [2] or 2.14×10^{13} ergs of energy. The S-IV B stage will impact the moon at a velocity of 2.58 km/sec, with a mass of 13 925 kg, therefore having an energy of 4.635×10^{17} ergs or 9.809×10^3 kg of TNT. Substituting these values into equation (1) results in a crater diameter of 13.48 meters for $k = 0.0312$ and 19.44 meters for $k = 0.0636$.

The United States Geological Survey studied the size of craters formed by missile impacts on various soils in 1966. In their report [3] 19 cases were published. Assuming that impact craters scale as the cube root of the energy, the 19 cases were scaled up to the energy of the S-IV B stage for the lunar impact. The scaled results are listed in Table 1.

The light gas gun facility performed six test shots using a solid aluminum cylinder to impact a simulated lunar soil sample of basalt made available by Dr. Costes of the Space Sciences Laboratory. A comparison of this soil to lunar soil is shown in Figure 1. The mass and velocity of the projectile were known and the depth and diameter of the crater were measured after impact. Using energy scaling to predict the size of the crater formed by the S-IV B impact into a similar soil, Table 2 was compiled.

Limited time in which to predict the crater size necessitated use of previously manufactured hardware. Therefore, the available area in which to conduct the experiments was restricted to 4 inches square. This may have contributed to the higher energy tests resulting in smaller craters. The restricted area prevented ejected soil from following a normal trajectory, causing some of it to refill the crater after initial processes had ceased.

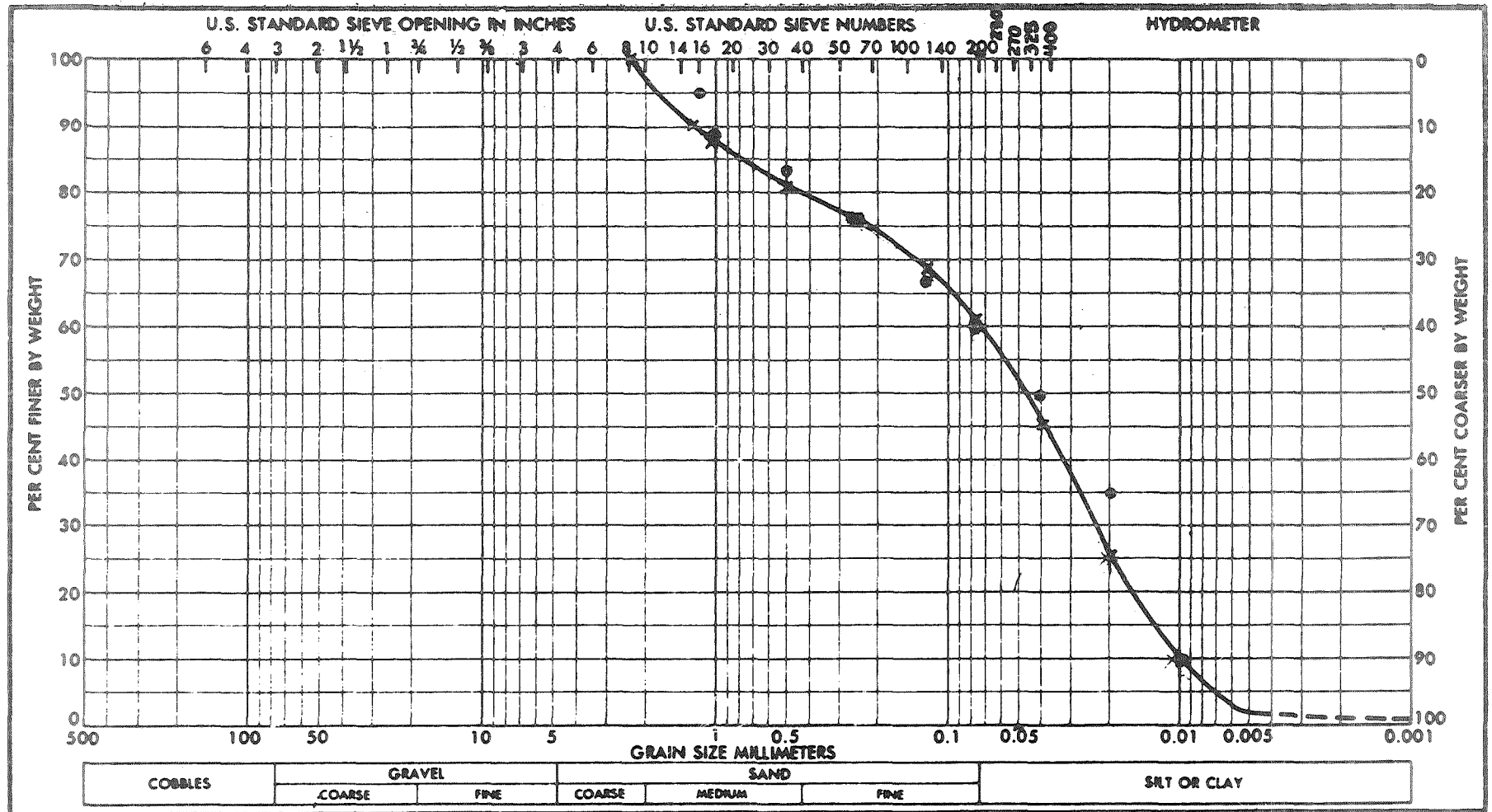
The three independent methods of predicting the impact crater for the S-IV B impact on the lunar surface give the following results:

TABLE 1. RESULTS SCALED TO AN ENERGY OF 4.635×10^{17} ERGS
FROM THE U. S. GEOLOGICAL SURVEY FOR CRATER SIZE^a

Target	Diameter (meters)	
	min	max
1. Sand, noncohesive	30.29	33.06
2. Sandstone, large cohesion	31.90	36.15
3. Gypsiferous Sediments, weakly cohesive	19.57	29.41
4. Aluvium, weakly cohesive	29.46	36.80
5. Gravelly Sands, weakly cohesive	25.28	29.21
6. Alluvium, weakly cohesive	32.35	41.58
7. Gypsum Lake Beds, cohesive, 20 percent water, density 1.2 - 1.6 g/cm ³	64.11	66.22
8. Alluvium, weakly cohesive	21.92	27.40
9. Colluvium, weakly cohesive	24.63	29.56
10. Gypsum Lake Beds, cohesive, 5 - 10 percent water, density 1.98 g/cm ³	31.03	40.04
11. Alluvium, weakly cohesive	20.90	31.35
12. Sand, weakly cohesive	24.11	28.93
13. Alluvium, weakly cohesive	35.77	36.61
14. Colluvium, weakly cohesive	37.08	37.55
15. Gypsum, cohesive	42.96	44.69
16. Gypsum Sand, cohesive	39.38	41.56
17. Clayie Silt, weakly cohesive ^b	39.66	43.35
18. Clayie, weakly cohesive	43.75	47.63
19. Soil and Colluvium Overlaying Clay and Siltstone, weakly cohesive	40.31	50.90
Average	21.59	38.58

a. The angle of impact from the U. S. Geological Survey was normalized while the S-IV B impact was only 5 degrees from normal so that normalization was ignored.

b. The clayie silt would probably approximate the lunar soil more closely from grain size considerations than the other soils listed.



• OFFICIAL LUNAR SOIL SPECIFICATION

× GRL SIMULANT

Figure 1. Lunar soil model GRL 11/16 versus official.

TABLE 2. TABLE OF CRATER SIZE USING ENERGY SCALING OF EACH OF SIX SHOTS, CONDUCTED BY THE LIGHT GAS GUN FACILITY

Shot Ref No.	Mass of Projectile m_p $\times 10^{-3}$ gm	Velocity of Projectile v_p $\times 10^5$ cm/sec	Kinetic Energy of Projectile E_p $\times 10^7$ ergs	Scaling Factor $\left(\frac{E_{IV}}{E_p}\right)^{1/3}$	Diameter of Crater Measured D_p cm	Diameter of Crater Expected D_{IV} meters
E-1-023	7.21	3.26	38.31	1065.56	4.44	47.31
E-1-024	7.22	3.40	41.73	1038.62	4.44	46.11
E-1-025	7.24	3.85	53.66	952.36	4.20	40.00
E-1-022	7.14	4.10	60.01	917.51	3.18	29.18
E-1-026	6.14	4.29	56.50	936.12	3.88	36.32
E-1-027	6.00	4.33	56.25	937.51	3.88	36.38

The average diameter of the three shots in 3 to 4 km/sec range is 44.47 meters.

The average diameter of the three shots in the 4 to 5 km/sec range is 33.96 meters.

		min	max
(1) Explosive formula		13.48	19.44
(2) Missile impacts	(avg)	21.59	38.53
	(clayie silt)	39.66	43.35
(3) Light gas gun experiments		29.18	47.31

The low prediction of the explosive formula may possibly be attributed to the lack of momentum consideration in the empirical development. That is, a traveling projectile has a given energy and momentum, while an explosive has only energy.

It was therefore concluded that the crater diameter formed by the S-IV B stage impact on the moon would approximate the physical impacts conducted under the other two studies. The predicted crater diameter is approximately 40 meters.

IMPACT FLASH

To determine if the impact flash could be observed from earth-based stations, the six light gas gun shots listed in Table 2 were monitored by two photomultiplier tubes. The viewing area of the tubes was 2.323 cm² at a distance of 10.95 cm from the impact point.

The maximum output voltage recorded by the photomultiplier tubes corresponded to a current of 2×10^{-5} amperes. The sensitivity of the photomultiplier tubes under the test conditions was 10 amperes/lumen, so that the luminosity recorded was 2×10^{-6} lumens. The total luminosity of the impact event is therefore:

$$L_p = \frac{(2 \times 10^{-6} \text{ lumens}) (10.95 \text{ centimeters})^2}{(2.323 \text{ cm}^2) \text{ steradians}} \frac{4 \pi \text{ steradians}}{\text{unit sphere}}$$

$$= 1.297 \times 10^{-3} \text{ lumens}$$

Three approaches were made, using this empirical information, to predict the maximum intensity of the flash to be generated by the S-IV B stage impact and find the magnitude.

1. Assume area scaling:

It was assumed that luminosity is directly proportional to the area of the impacting body.

The diameter of the base of the S-IV B stage (660 cm) was used, because a maximum flash would be generated in this orientation. The scale factor a is:

$$a = \frac{A_{IV}}{A_p} = \frac{\frac{\pi d_{IV}^2}{4}}{\frac{\pi d_p^2}{4}} = \frac{d_{IV}^2}{d_p^2} = \frac{(660 \text{ cm})^2}{(0.165 \text{ cm})^2} = 1.60 \times 10^7$$

$$L_{IV} = a L_p = 2.075 \times 10^4 \text{ lumens}$$

At earth distance, the intensity is:

$$I = \frac{L_{IV}}{4 \pi r_E^2} = 1.12 \times 10^{-18} \text{ lumens/cm}^2$$

where r_E is the distance between the earth and the moon (3.84×10^{10} cm).

To determine the magnitude we use the equation [4]

$$-2.5 \log_{10} \left(\frac{I}{I_0} \right) = M_V$$

where I_0 is the intensity of a zero magnitude star (2.65×10^{-10} lumens/cm²).

Using the intensity calculated from the empirical work, we find:

$$M_V = 20.94$$

Therefore, the impact flash generated by the S-IV B stage impact on the lunar surface, based on the laboratory data and area scaling, would be equivalent to approximately a 21st magnitude star.

2. Assume mass scaling:

$$a = \frac{M_{IV}}{M_p} = \frac{13.925 \times 10^6 \text{ gms}}{6.825 \times 10^{-3} \text{ gms}} = 2.04 \times 10^9$$

$$L = 2.646 \times 10^6 \text{ lumens}$$

$$I = 1.428 \times 10^{-16} \text{ lumens/cm}^2$$

and

$$M_v = 15.67$$

3. Assume energy scaling:

$$a = \frac{E_{IV}}{E_p} = \frac{4.635 \times 10^{17} \text{ ergs}}{5.366 \times 10^8 \text{ ergs}} = 8.638 \times 10^8$$

$$L = 1.12 \times 10^6 \text{ lumens}$$

$$I = 6.05 \times 10^{-17} \text{ lumens/cm}^2$$

and

$$M_v = 16.60$$

CONCLUSIONS

An attempt was made to predict the crater size and impact flash created by the Apollo 13 S-IV B stage impact on the lunar surface. Both theory and empirical results were used to obtain a meaningful result.

The crater size is predicted to be approximately 40 meters in diameter. This prediction is based on results obtained using an explosive formula, missile impacts on various soils, and experiments conducted using a light gas gun facility.

The maximum flash expected is based on the empirical information gained in the light gas gun experiments and scaling. The three scaling factors and the calculated results are:

<u>Scaling Factors</u>	<u>Equivalent Order Magnitude Star</u>
area scaling	21
mass scaling	16
energy scaling	17

Therefore the maximum flash expected would be equivalent to a 16th magnitude star.

On two of the six laboratory impacts some glassy spheres were found that are similar to the spheres found in the Apollo 11 lunar soil sample. Details of soil examination after impact experiments are contained in the Appendix.

APPENDIX

At the beginning of the experiments in the light gas gun facility it was decided that after each crater had been measured and photographed, the top layer of soil that surrounded and lined the crater would be sifted and examined to determine if remains of the projectile could be found.

While examining the first sample some spheres were found. These spheres, shown in Figure A-1, show evidence of melting and fusion. They are similar to spheres found in the actual lunar soil from Apollo 11 shown in Figure A-2, and the soil material when examined under a microscope is very similar to the actual moon soil sample. There are irregular shaped fragments of basalt ranging from clear fragments, similar to the one to which one of the spheres in Figure A-1 is fused, to dark opaque fragments.

The sieves used for separating the soil sample had been examined before this part of the experiment to be sure that they contained no foreign material; however, it was concluded that this examination was not so rigorous as to preclude all possibilities of contamination. The sieves had been used to separate and obtain uniform glass spheres in other experiments. Therefore, the possibility that the spheres were a result of this form of contamination was considered; although it was unlikely that a sphere of this size would be missed in the preliminary examination.

The top four inches of the remaining sample was examined and produced no additional spheres. Communication with Dr. Costes of Space Sciences Laboratory, from whom the sample was obtained, gave assurance that there were no such objects introduced into the soil by the manufacturer.

The next three shots were examined in an identical manner. No spheres were found. However, during the examination of the fifth shot three more spheres, shown in Figure A-3, were found. Again the spheres came from the soil which surrounded and lined the crater. No spheres were found on the sixth shot. The shot reference number associated with the two tests in which spheres were found are E-1-022 and E-1-026. From Table 2 it was noted that these two shots were adjacent in the velocity and energy variations of the test series. The range used for this test series had a 10.16 cm square free flight path, 182.88 cm in length, to check the velocity of the primary projectile. The range was vertical and examination of the inside of the range showed that many of the soil fragments ejected from the crater area had traveled a vertical height of greater than 1 meter. This allowed approximately 1 second of free fall for molten ejecta to solidify.

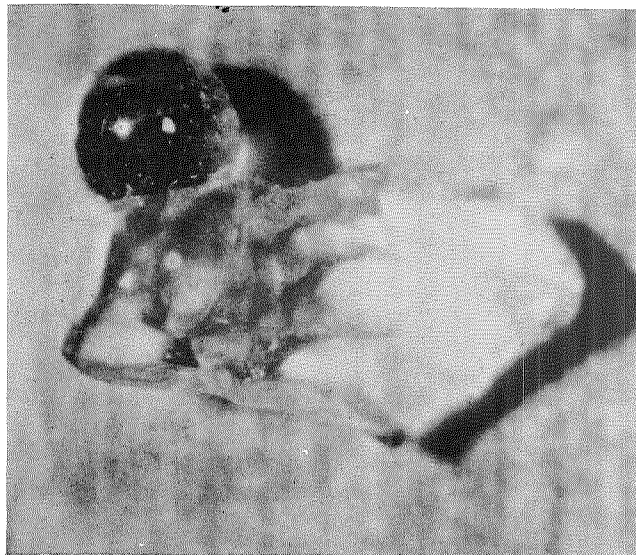
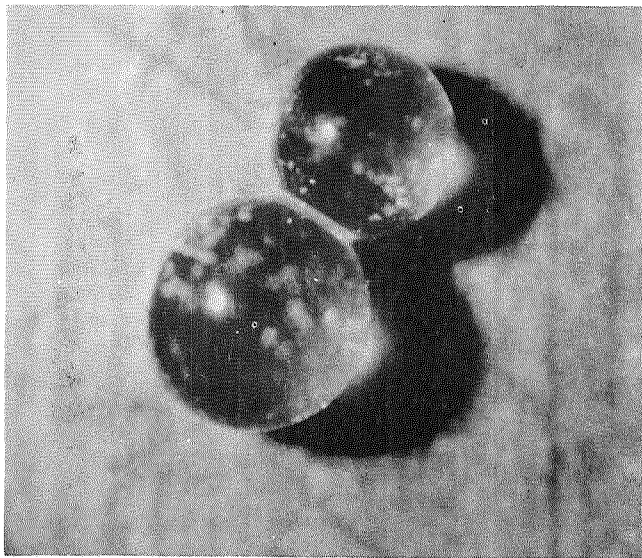


Figure A-1. Glassy spheres found on shot reference number E-2-022.



Figure A-2. Apollo 11 loose lunar soil sample (TN12, Manned Spacecraft Center).

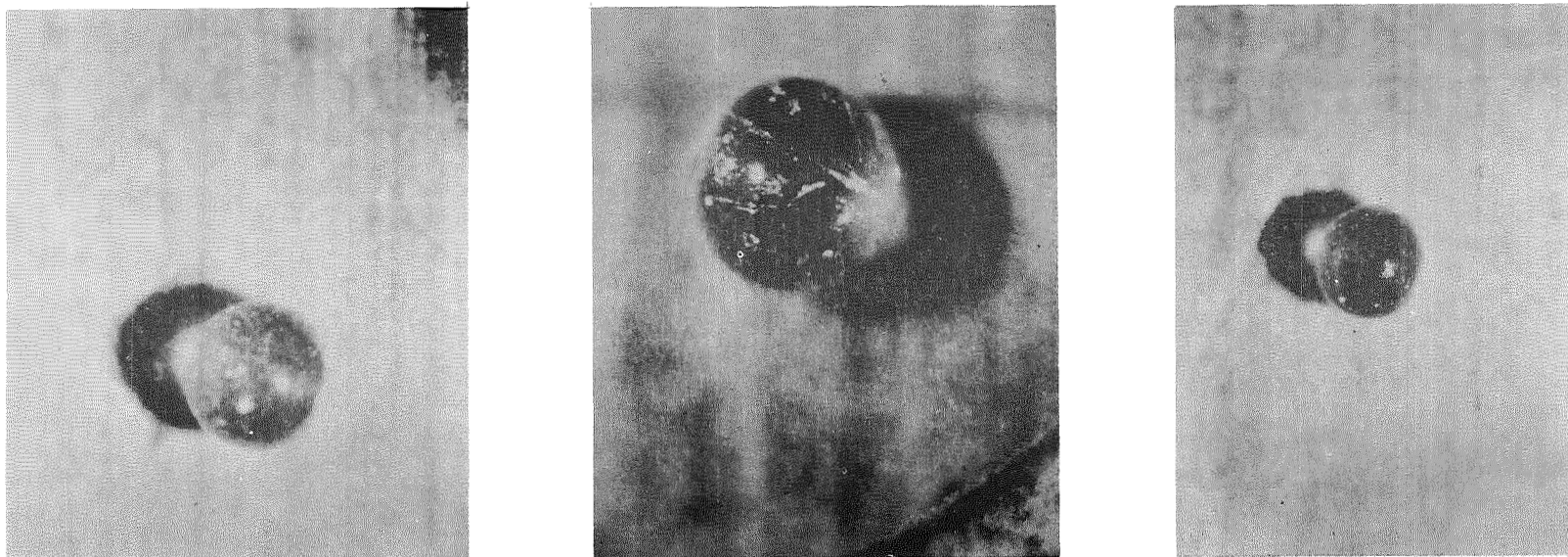


Figure A-3. Glassy spheres found on shot reference number E-2-026.

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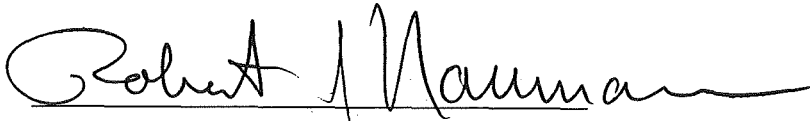
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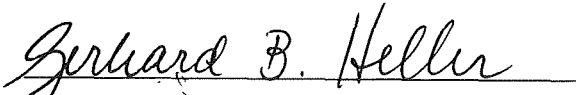
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